

Geometry - GT/Honors
Chapter 6 Review - Quadrilaterals

Name _____
Date _____ Period _____

Find each of the following values.

Use parallelogram GRAM for problems 1-4.

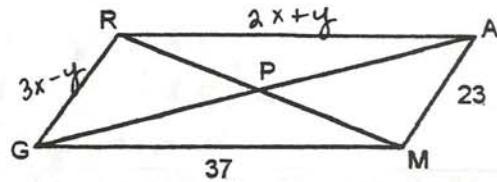
50

1. $GA = 3x - 10$ and $GP = x + 20$. Find x .

$$2(x+20) = 3x - 10$$

$$2x + 40 = 3x - 10$$

$$50 = x$$



58

2. $m\angle GMR = 37^\circ$ and $m\angle AMG = 95^\circ$, find $m\angle GRM$.

$$\begin{array}{r} 95 \\ - 37 \\ \hline 58 \end{array}$$

105

3. $m\angle RGM = 75^\circ$, find $m\angle GMA$

$$\begin{array}{r} 180 \\ - 75 \\ \hline 105 \end{array}$$

x = 12

4. $RA = 2x + y$, $GR = 3x - y$, find x and y

y = 13

$$2x + y = 37$$

$$x = 12$$

$$24 + y = 37$$

$$3x - y = 23$$

$$5x = 60$$

$$y = 13$$

$$3x - 23 = y$$

$$5x = 60$$

$$2x + (3x - 23) = 37$$

$$x = 12$$

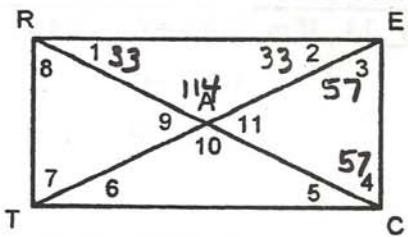
Use rectangle RECT for problems 5-8.

9

5. If $TA = 3x - 7$ and $AC = 2x + 2$, find x .

$$3x - 7 = 2x + 2$$

$$x = 9$$



6

6. If $m\angle 2 = 33^\circ$, find $m\angle 11$.

8

7. If $RT = 2x + 5$ and $EC = 4x - 11$, find x .

$$2x + 5 = 4x - 11$$

$$16 = 2x$$

$$8 = x$$

-7, 6

8. If $m\angle 1 = x^2 - 4$ and $m\angle 8 = x + 52$, find x .

$$32$$

$$58$$

$$x^2 - 4 + x + 52 = 90$$

$$x^2 + x + 48 = 90$$

$$x^2 + x - 42 = 0$$

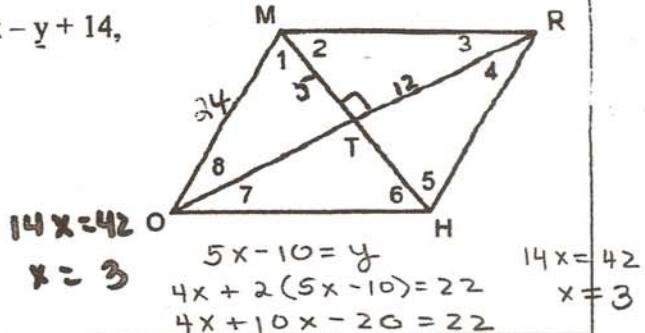
$$(x+7)(x-6) = 0$$

$$x = -7 \quad x = 6$$

Use rhombus RHOM for problems 9-11.

$x = 3$ 9. If $MO = 24$, $MR = 4x + 2y + 2$, and $RH = 5x - y + 14$,

$y = 5$ find x and y .
 $4x + 2y + 2 = 24$
 $5x - y + 14 = 24$
 $4x + 2y = 22$
 $2(5x - y = 10)$
 $10x - 2y = 20$



13. 10. If $RO = 24$ and $MH = 10$, find MR .

$TR = 12$ $MT = 5$
 $5^2 + 12^2 = x^2$
 $x = 13$

51. 11. If $m\angle 7 = 39^\circ$, find $m\angle 2$.

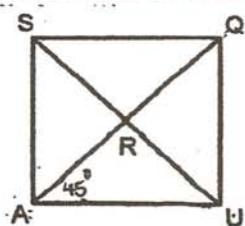
$$\begin{array}{r} 90 \\ - 39 \\ \hline 51 \end{array}$$

Use square SQUA for problems 12-14.

2, 3. 12. If $AU = x^2 + 2$ and $SA = 5x - 4$, find x

$x^2 + 2 = 5x - 4$
 $x^2 - 5x + 6 = 0$
 $(x-2)(x-3) = 0$

$x-2=0$ $x-3=0$
 $x=2$ $x=3$



15. 13. If $m\angle ARS = 6x$, find x .

$6x = 90$
 $x = 15$

19. 14. $m\angle QAU = 3x - 12$, find x .

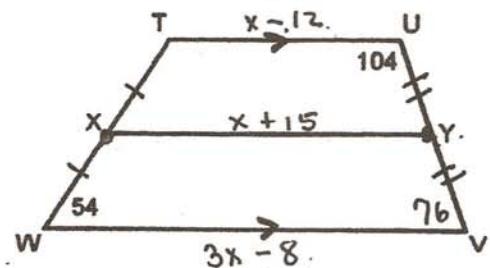
$3x - 12 = 45$
 $3x = 57$
 $x = 19$

$90 + 6x - 24 = 180$
 $6x - 24 = 90$
 $6x = 114$
 $x = 19$

Use trapezoid TUVW with median XY for problems 15-17.

76. 15. $m\angle V$

24. 16. $TU = 15$, $WV = 33$, find XY . $\frac{15+33}{2} = \frac{48}{2}$



25. 17. $TU = x - 12$, $XY = x + 15$, $WV = 3x - 8$, find x .

$\frac{x-12 + 3x-8}{2} = x + 15$

$4x - 20 = 2x + 30$
 $2x = 50$

Use isosceles trapezoid TRAP for problems 18-20.

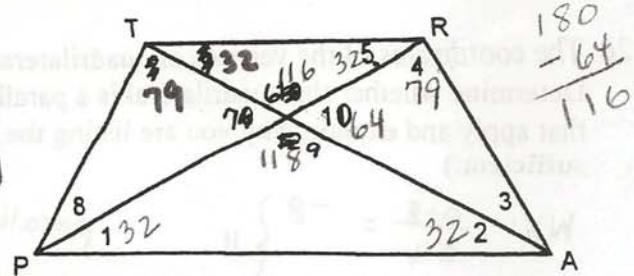
$$\underline{32} \quad 18. m\angle 1$$

$$\begin{array}{r} 79 \\ 64 \\ \hline 143 \end{array} \quad \begin{array}{r} 180 \\ -143 \\ \hline 37 \end{array}$$

$m\angle 6 = 32^\circ$
 $m\angle 7 = 79^\circ$

$$\underline{64} \quad 19. m\angle 7$$

$$\underline{37} \quad 20. m\angle 3$$



In problems 21-23, if there is enough information to state that the quadrilateral is a parallelogram give the reason. Write none if there is not enough information to state that the quadrilateral is a parallelogram.

21. E is the midpoint of \overline{AC} and \overline{BD}

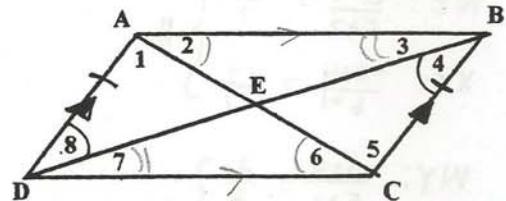
diagonals bisect each other $\rightarrow \square$

22. $\angle 2 \cong \angle 6$ and $\angle 3 \cong \angle 7$

none, only one pair of opp sides \parallel

23. $\angle 8 \cong \angle 4$ and $\overline{AD} \cong \overline{BC}$

one pair opp sides \cong and $\parallel \rightarrow \square$

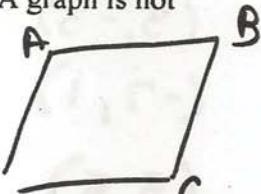


24. The coordinates of the vertices of quadrilateral ABCD are A(-4, -2), B(-1, 3), C(4, 0), and D(1, -5).

Determine whether the quadrilateral is a parallelogram, a rectangle, a rhombus, or a square. List all that apply and explain why you are listing the ones that you are. SHOW WORK! (A graph is not sufficient.)

$$\begin{aligned} m\overline{AB} &= \frac{5}{3} \\ m\overline{DC} &= \frac{5}{3} \\ m\overline{AD} &= -\frac{3}{5} \\ m\overline{BC} &= -\frac{3}{5} \end{aligned} \quad \left. \begin{aligned} &\parallel \\ &\parallel \\ &\perp \\ &\parallel \right\}$$

$$\begin{aligned} m\overline{AC} &= \frac{1}{4} \\ m\overline{BD} &= -4 \end{aligned} \quad \left. \begin{aligned} &\perp \\ &\perp \end{aligned} \right\}$$



parallelogram (opp sides \parallel)
rectangle (parallelogram with adj sides \perp)
rhombus (\square with \perp diagonals)
square (both rectangle & rhombus)

25. The coordinates of the vertices of quadrilateral PQRS are P(4, 4), Q(1, 2), R(2, -2), and S(5, 0).

Determine whether the quadrilateral is a parallelogram, a rectangle, a rhombus, or a square. List all that apply and explain why you are listing the ones that you are. SHOW WORK! (A graph is not sufficient.)

$$\begin{aligned} m\overline{PQ} &= \frac{2}{3} \\ m\overline{SR} &= \frac{2}{3} \end{aligned} \quad \left. \begin{aligned} &\parallel \\ &\text{not } \perp \end{aligned} \right\}$$

$$\begin{aligned} m\overline{PS} &= -4 \\ m\overline{QR} &= -4 \end{aligned} \quad \left. \begin{aligned} &\parallel \\ &\parallel \end{aligned} \right\}$$

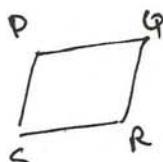
$$\begin{aligned} m\overline{PR} &= 3 \\ m\overline{QS} &= -\frac{1}{2} \end{aligned} \quad \left. \begin{aligned} &\text{not } \perp \\ &\perp \end{aligned} \right\}$$

parallelogram
(opp sides \parallel)

rectangle - no
adj. sides not \perp

rhombus - no
diag not \perp

square - no
not rect & rhomb



$$PR = \sqrt{2^2 + 6^2} = \sqrt{40}$$

$$QS = \sqrt{4^2 + 2^2} = \sqrt{20}$$

$$PQ = \sqrt{3^2 + 2^2} = \sqrt{13}$$

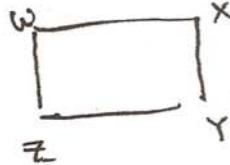
$$QR = \sqrt{1^2 + 4^2} = \sqrt{17}$$

26. The coordinates of the vertices of quadrilateral WXYZ are W(5, 0), X(6, -8), Y(-1, -4), and Z(-2, 4). Determine whether the quadrilateral is a parallelogram, a rectangle, a rhombus, or a square. List all that apply and explain why you are listing the ones that you are. SHOW WORK! (A graph is not sufficient.)

$$\begin{aligned}WX: \frac{0+8}{5-6} &= -8 \quad \left. \begin{array}{l} \\ \end{array} \right\} \parallel \\ZY: \frac{-4-4}{-1+2} &= -8 \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{not } \perp \\WZ: \frac{0-4}{5+2} &= -\frac{4}{7} \quad \left. \begin{array}{l} \\ \end{array} \right\} \parallel \\XY: \frac{-8+4}{6+1} &= -\frac{4}{7}\end{aligned}$$

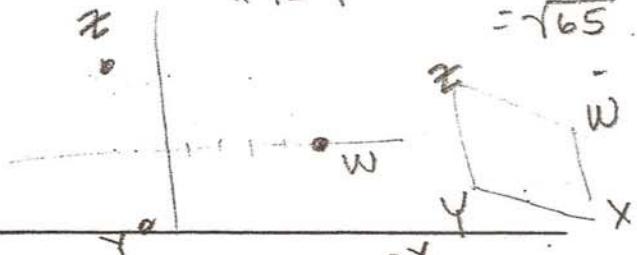
parallelogram (opp sides \parallel)
rhombus (diagonals \perp)
rectangle (no-adj. sides
 $\text{not } \perp$)

square - no - not rect.



$$WX = \sqrt{1^2 + 8^2} = \sqrt{65}$$

$$XY = \sqrt{7^2 + 4^2} = \sqrt{49 + 16} = \sqrt{65}$$

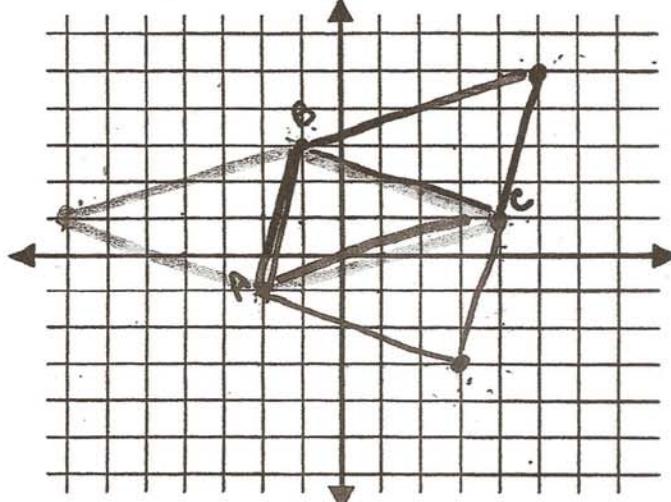


27. Find the coordinates of the 3 possible points for the missing vertex in a parallelogram if three of the vertices are $(-2, -1)$, $(-1, 3)$, and $(4, 1)$.

$$(3, -3) \text{ ABCD}$$

$$(-7, 1) \text{ ADBC}$$

$$(5, 5) \text{ ABDC}$$

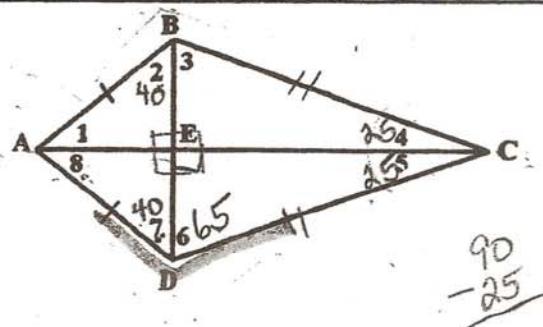


28. Given ABCD is a kite and $m\angle BCD = 50^\circ$
 $m\angle 2 = 40^\circ$
 $ED = 6$

$$\text{find } m\angle 8 = 50$$

$$m\angle ADC = 105$$

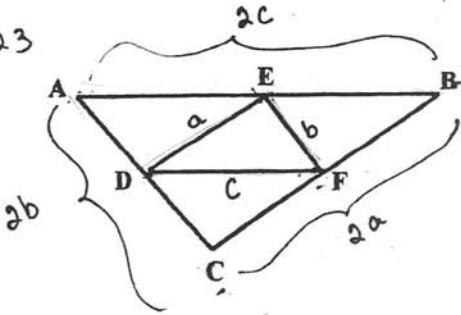
$$BD = 12$$



$$a+b+c = 23$$

29. $\triangle ABC$ has midpoints D, E, and F. If the perimeter of $\triangle DEF$ is 23, then find the perimeter of $\triangle ABC$.

46



30. KITE is a kite. M, N, O, and P are midpoints.

$$m\angle KMN = 30$$

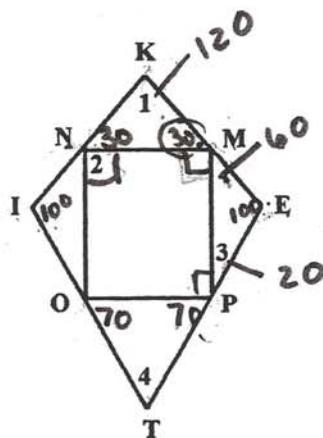
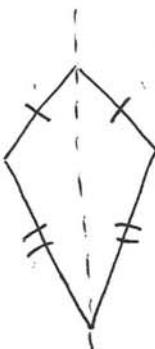
$$m\angle KIT = 100$$

Find: $m\angle 1 = \underline{\hspace{2cm}} \text{ } 120$

$$m\angle 2 = \underline{\underline{90}}$$

$$m\angle 3 = \underline{20}$$

$$m\angle 4 = \underline{\hspace{2cm}40}$$



$$\begin{array}{r} 120 \\ 100 \\ \hline 220 \end{array}$$

31. OE is an isosceles trapezoid. T, R, A, and P are midpoints

$$IO = 12$$

$$m\angle RIT = 75^\circ \text{ and } m\angle SRA = 40^\circ$$

Find: $m\angle 1 =$ 35

$$m\angle 2 = \underline{\hspace{2cm}} 70$$

$$m\angle 3 = \underline{\hspace{2cm}} 35.$$

$$RA = \underline{\underline{6}}$$

$$AP = 6$$

