

Geometry Worksheet
**Equations of medians, altitudes
& perpendicular bisectors**

Name _____ Date _____ Period _____

(KEY)

The vertices of $\triangle ABC$ are $A(2, 18)$, $B(-2, -4)$, and $C(6, 12)$

1. Find the slope of \overline{AB} . $\frac{-4-18}{-2-2} = \frac{-22}{-4} = \boxed{\frac{11}{2}}$	2. Find the slope of \overline{BC} . $\frac{12+4}{6+2} = \frac{16}{8} = \boxed{2}$	3. Find the slope of \overline{AC} . $\frac{12-18}{6-2} = \frac{-6}{4} = \boxed{-\frac{3}{2}}$
4. Write the equation of the line containing \overline{AB} . $m = \frac{11}{2} A(2, 18) B(-2, -4)$ $y - 18 = \frac{11}{2}(x - 2) \quad \text{or}$ $y + 4 = \frac{11}{2}(x + 2)$	5. Write the equation of the line containing \overline{BC} $m = 2 B(-2, -4) C(6, 12)$ $y + 4 = 2(x + 2) \quad \text{or}$ $y - 12 = 2(x - 6)$	6. Write the equation of the line containing \overline{AC} $m = -\frac{3}{2} A(2, 18) C(6, 12)$ $y - 18 = -\frac{3}{2}(x - 2) \quad \text{or}$ $y - 12 = -\frac{3}{2}(x - 6)$
7. Find the equation of the line containing the altitude from C to \overline{AB} . $\perp m = -\frac{2}{11} C(6, 12)$ $y - 12 = -\frac{2}{11}(x - 6)$	8. Write the equation of the line containing the altitude from A to \overline{BC} . $A(2, 18)$ $\perp m = -\frac{1}{2}$ $y - 18 = -\frac{1}{2}(x - 2)$	9. Find the equation of the line containing the altitude from B to \overline{AC} . $B(-2, -4)$ $\perp m = \frac{2}{3}$ $y + 4 = \frac{2}{3}(x + 2)$
10. Find the coordinates of the midpoint of \overline{AB} . $\left(\frac{2-2}{2}, \frac{18-4}{2}\right) = \boxed{(0, 7)}$	11. Find the coordinates of the midpoint of \overline{BC} . $\left(\frac{-2+6}{2}, \frac{-4+12}{2}\right) = \boxed{(2, 4)}$	12. Find the coordinates of the midpoint of \overline{AC} . $\left(\frac{2+6}{2}, \frac{18+12}{2}\right) = \boxed{(4, 15)}$
13. Find the equation of the line containing the median from C to \overline{AB} . $C(6, 12) (0, 7)$ $m = \frac{7-12}{0-6} = \frac{-5}{-6} = \frac{5}{6}$ $y - 12 = \frac{5}{6}(x - 6) \quad \text{or}$ $y = \frac{5}{6}x + 7$	14. Find the equation of the line containing the median from A to \overline{BC} . $(2, 18) (2, 4)$ $X = 2$	15. Find the equation of the line containing the median from B to \overline{AC} . $(-2, -4) (4, 15)$ $m = \frac{15+4}{4+2} = \frac{19}{6}$ $y + 4 = \frac{19}{6}(x + 2) \quad \text{or}$ $y - 15 = \frac{19}{6}(x - 4)$

16. Find the equation of the line containing the perpendicular bisector of \overline{AB} (0, 7)

$$\perp m = -\frac{1}{3} \text{ mid.}$$

$$y = -\frac{1}{3}x + 7$$

17. Find the equation of the line containing the perpendicular bisector of \overline{BC} (2, 4)

$$\perp m = -\frac{1}{2}$$

$$y - 4 = -\frac{1}{2}(x - 2)$$

18. Find the equation of the line containing the perpendicular bisector of \overline{AC} (4, 15)

$$\perp m = \frac{2}{3}$$

$$y - 15 = \frac{2}{3}(x - 4)$$

Given: R(0, 10), S(-5, 0), and T(5, 5). Write the equation of:

19. the median from R

$$\text{midpoint } \overline{RT} = \left(0, \frac{5}{2}\right)$$

$$R(0, 10)$$

$$x = 0$$

20. the median from S

$$\text{mid. of } \overline{RT} \left(\frac{5}{2}, \frac{7}{2}\right)$$

$$S(-5, 0)$$

$$\text{Median slope: } -\frac{3.5}{-7.5} = \frac{7}{15}$$

$$y - \frac{7}{2} = \frac{7}{15}(x - \frac{5}{2}) \text{ or}$$

$$y = \frac{7}{15}(x + 5)$$

21. the median from T(5, 5)

$$\text{mid } \overline{RS} (-\frac{5}{2}, 5)$$

$$y = 5$$

22. the altitude from T

$$\text{slope of } \overline{RS} = 2$$

$$\perp m = -\frac{1}{2} T(5, 5)$$

$$y - 5 = -\frac{1}{2}(x - 5)$$

23. the altitude from R

$$\text{slope } \overline{ST} = \frac{1}{2}; \perp m = -2$$

$$y = -2x + 10$$

24. the altitude from S(-5, 0)

$$\text{slope } \overline{RT} = -1$$

$$y = -(x + 5)$$

$$\text{or}$$

$$y = -x - 5$$

25. the perpendicular bisector of segment RS

$$\text{midpoint } \overline{RS} \left(-\frac{5}{2}, 5\right)$$

$$\perp m = -\frac{1}{2}$$

$$y - 5 = -\frac{1}{2}(x + \frac{5}{2})$$

26. the perpendicular bisector of segment ST

$$\text{midpoint } \overline{ST} \left(0, \frac{5}{2}\right)$$

$$\text{slope } \overline{ST} = \frac{1}{2}; \perp m = -2$$

$$y = -2x + \frac{5}{2}$$

27. the perpendicular bisector of segment RT

$$\perp m \overline{RT} = 1 \quad \left(\frac{5}{2}, \frac{7}{2}\right)$$

$$\text{mid } \overline{RT}$$

$$y - \frac{7}{2} = 1(x - \frac{5}{2})$$

$$\text{or}$$

$$y - \frac{7}{2} = x - \frac{5}{2}$$